A component based noise correction method (CompCor) for BOLD and perfusion based fMRI

Yashar Behzadi,a,b Khaled Restom,a Joy Liau,a,b and Thomas T. Liu*a,

aUCSD Center for Functional Magnetic Resonance Imaging and Department of Radiology, 9500 Gilman Drive, MC 0677, La Jolla, CA 92037-0677, USA

bDepartment of Bioengineering, University of California San Diego, La Jolla, CA, USA

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A component based method (CompCor) for the reduction of noise in both blood oxygenation level-dependent (BOLD) and perfusion-based functional magnetic resonance imaging (fMRI) data is presented. In the proposed method, significant principal components are derived from noise regions-of-interest (ROI) in which the time series data are unlikely to be modulated by neural activity. These components are then included as nuisance parameters within general linear models for BOLD and perfusion-based fMRI time series data. Two approaches for the determination of the noise ROI are considered. The first method uses high-resolution anatomical data to define a region of interest composed primarily of white matter and cerebrospinal fluid, while the second method defines a region based upon the temporal standard deviation of the time series data. With the application of CompCor, the temporal standard deviation of resting-state perfusion and BOLD data in gray matter regions was significantly reduced as compared to either no correction or the application of a previously described retrospective image based correction scheme (RETROICOR). For both functional perfusion and BOLD data, the application of CompCor significantly increased the number of activated voxels as compared to no correction. In addition, for functional BOLD data, there were significantly more activated voxels detected with CompCor as compared to RETROICOR. In comparison to RETROICOR, CompCor has the advantage of not requiring external monitoring of physiological fluctuations.

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Introduction

Over the last decade, blood oxygenation level-dependent (BOLD) and perfusion-based functional magnetic resonance imaging (fMRI) have become indispensable tools for studies of the working brain. When utilized together, the BOLD and perfusion signals can provide a quantitative understanding of the metabolic response to neural activity and provide insight into neurovascular coupling mechanisms (Hoge et al., 1999). However, as the fMRI community has moved to higher field strengths, physiological noise has become an increasingly important confound limiting the sensitivity and the application of fMRI studies (Kruger and Glover, 2001; Liu et al., 2006).

Physiological fluctuations have been shown to be a significant source of noise in BOLD fMRI experiments, with an even greater effect in perfusion-based fMRI utilizing arterial spin labeling (ASL) techniques (Kruger and Glover, 2001; Restom et al., 2006). Physiological sources of noise primarily include cardiac pulsations and respiratory-induced modulations of the main magnetic field. Additional sources include blood flow changes coupled to end-tidal CO2 and vasomotion occurring at 0.1 Hz (Hu et al., 1995; Dagli et al., 1999; Glover et al., 2000a).

Approaches to removing cardiac and respiratory related noise include temporal filtering, image-based retrospective correction (RETROICOR), k-space-based correction (RETROKCOR) and navigator echo-based correction (DORK) (Hu et al., 1995; Biswal et al., 1996; Josephs et al., 1997; Glover et al., 2000a; Pfeuffer et al., 2002). More recently, RETROICOR has been extended to a general linear model (GLM) framework (Lund et al., 2006) and modified for use in ASL studies (Restom et al., 2006). A recent adaptation for BOLD-based imaging employs additional regressors describing variations in respiratory volume (Birn et al., 2006).

An alternate approach to the use of external measures of physiological activity or specially modified pulse sequences is to globally subtract average time courses from regions unlikely to be associated with neural activity, such as ventricles and large vessels (Petersen et al., 1998; Lund and Hanson, 2001). However, since this technique removes only the average time series, it is unable to account for voxel-specific phase differences in the noise due to physiological fluctuations. Additionally, component-based techniques, utilizing independent component analysis (ICA) or principal component analysis (PCA), have shown potential in identifying spatial and temporal patterns of structured noise (Thomas et al., 2002; McKeown et al., 2003; Beckmann and Smith, 2004). However, the utility of component-based methods has been limited to BOLD studies with sampling times short enough to clearly differentiate cardiac and respiratory elements from evoked responses (Thomas et al., 2002), in
which case a temporal band pass filter would be adequate for noise removal.

In this paper we present and characterize a novel component-based method (CompCor) for the correction of physiological noise in BOLD and perfusion-based fMRI. We show that principal components derived from noise regions-of-interest (ROI) are able to accurately describe physiological noise processes in gray matter regions. In our presentation we investigate the use of two different methods for determining noise ROIs. The first method uses anatomical data to identify white matter and CSF voxels, while the second method uses the temporal standard deviation (tSTD) of the time series data to identify voxels dominated by physiological noise. We show that the use of principal components derived from a noise ROI as nuisance regressors in a GLM of the fMRI signal can significantly reduce the temporal standard deviation in resting-state scans and increase the sensitivity of functional BOLD and perfusion-based studies.

Theory

CompCor algorithm

The underlying assumption in the CompCor algorithm is that signal from a noise ROI can be used to accurately model physiological fluctuations in gray matter regions. The term “noise ROI” refers to areas (e.g., white matter, ventricles, large vessels) in which temporal fluctuations are unlikely to be modulated by neural activity and are primarily a reflection of physiological noise. The ability to model gray matter physiological noise elements is then predicated on the similarity between physiological fluctuations in the noise ROI and gray matter. A principal component analysis (PCA) is used to compactly characterize the time series data from the noise ROI. Significant principal components are then introduced as covariates in a general linear model (GLM) as an estimate of the physiological noise signal space.

In this paper we investigate the use of two methods for determining the noise ROI. The first method uses anatomical data to identify voxels that consist primarily of either white matter or cerebrospinal fluid (CSF). Since neural activation is localized to gray matter, fluctuations in white matter and CSF regions should primarily reflect signals of non-neural origin, such as cardiac and respiratory fluctuations.

In the second method, voxels with high temporal standard deviation (tSTD) are used to define a noise ROI. This approach is based on previous preliminary work by Lund et al. (2001) in which areas of high temporal standard deviation were found to correspond to ventricles, edge regions, and vessels. The advantage of this method is that it utilizes the time series data to identify a noise ROI without the need for an anatomical scan.

General linear model for ASL and BOLD

The general linear model for the BOLD-weighted data can be written as

\[
b = Xh + Sd + Pc + n
\]

where \(b\) represents the measured BOLD data, \(Xh\) represents the stimulus response where \(X\) is a \(N \times k\) design matrix and \(h\) is a \(k \times 1\) vector of hemodynamic parameters. In the case of a block design, \(X\) reduces to a vector containing the smoothed stimulus pattern and \(h\) reduces to a scalar representing the unknown amplitude. Nuisance parameters are integrated in \(Sd\), where \(S\) is a \(N \times l\) matrix comprised of \(l\) nuisance model functions and \(d\) is a \(l \times 1\) vector of nuisance parameters. We have also added physiological noise terms \(Pc\) where \(P\) is a \(N\times m\) matrix containing \(m\) regressors and \(c\) represents the unknown regressor weights. Finally, \(n\) represents the additive noise term.

A general linear model (GLM) for ASL data in gray matter can be written as

\[
p = Xh_{\text{BOLD}} + MXh_{\text{perf}} + Sd + Pc + n
\]

where \(p\) is the acquired raw data representing interleaved tag and control images. In this model, the term modeling perfusion \(Xh_{\text{perf}}\) is modulated by a diagonal matrix, \(M\), consisting of alternating –1s and 1s for the tag and control images, respectively (Mumford et al., 2006; Restom et al., 2006). The term \(Xh_{\text{BOLD}}\) models a BOLD weighted static tissue component.

In a noise ROI, where we expect no stimulus-related response, the GLM reduces to \(b = Sd + Pc + n\) or \(p = Sd + Pc + n\) for BOLD and perfusion data, respectively. An assumption of CompCor is that the space spanned by the significant principal components from the noise ROI can be used to estimate the space spanned by the columns of the physiological regressor matrix \(P\).

![Fig. 1. Schematic of the CompCor algorithm in which significant principal components from a noise ROI are used to form a physiological noise ROI General Linear Model](image)

1) Anatomical noise ROI - White matter and CSF only voxels
2) tSTD noise ROI - Top 2% of voxels per slice with highest temporal standard deviation

Fig. 1. Schematic of the CompCor algorithm in which significant principal components derived from time series data within noise regions-of-interest (nROI) are used to form an estimate \(P_{\text{est}}\) of the physiological noise matrix \(P\). Incorporation of \(P_{\text{est}}\) into the general linear model for the signal in gray matter allows for estimation and removal of physiological fluctuations.
noise matrix $P_{\text{est}}$, which is then used as an estimate of $P$ in the GLM. For functional studies, an added processing step is included to minimize the possibility of including stimulus related fluctuations. In this step, a preliminary GLM analysis, using the appropriate design matrix $X$, is used to exclude voxels from the noise ROI with a calculated $p$-value less than 0.2. Additional details are provided in the Methods section.

**Methods**

**Experimental protocol**

Ten healthy subjects (ages 23 to 39) participated in the study after giving informed consent. Each subject viewed one periodic single trial visual stimulus consisting of a 20-s initial “off” period followed by 5 cycles of a 4-s “on” period and a 40-s “off” period. In addition to a periodic design, each subject viewed one block design consisting of 4 cycles of a 20-s “on” period and a 40-s “off” period. During the “on” periods, a full-field, full contrast radial 8-Hz flickering checkerboard was displayed, while the “off” periods consisted of a gray background of luminance equal to the average luminance of the “on” period. All subjects also underwent two resting-state scans (one for perfusion and one for BOLD), during which the subject was presented with the “off” condition for 3 min.

**Imaging protocol**

Imaging data were collected on a GE Signa Excite 3-T whole body system with a body transmit coil and an eight-channel receive coil. During the perfusion resting-state scan and the block design scan, data were acquired with a PICORE QUIPPS II (Wong et al., 1998) arterial spin labeling (ASL) sequence (TR=2 s, TI1/TI2=600/1500 ms, 10-cm tag thickness, and a 1-cm tag-slice gap) with a dual echo spiral readout (TE1/TE2=9.1/30 ms, FOV=24 cm, 64×64 matrix, and a flip angle=90°). Small bipolar crusher gradients were included to reduce signal from large vessels ($b=2 \text{ s/mm}^2$). Three oblique axial 8-mm slices were prescribed about the calcarine sulcus for this ASL run. The first echo data were used for the analysis of the perfusion response and are referred to as the ASL or perfusion signal, while the second echo data were used for the analysis of the BOLD response and are referred to as the 2nd echo BOLD signal. During the periodic single trial runs, BOLD-weighted images were acquired with a spiral readout (TE=25 ms, TR=500 ms, FOV=24 cm, 64×64 matrix, and a flip angle of 45°) and the same slice prescription as the ASL runs. The second resting-state scan was acquired with the following BOLD imaging parameters (TE=25 ms, TR=250 ms, FOV=24 cm, 64×64 matrix, and a flip angle of 40°).

A high-resolution structural scan was acquired with a magnetization-prepared 3D fast spoiled gradient acquisition in the steady-state (FSPGR) sequence (TI 450 ms, TR 7.9 ms, TE 3.1 ms, 12° flip angle, FOV 25×25×16 cm, matrix 256×256×124).

Cardiac pulse and respiratory effort data were monitored using a pulse oximeter (InVivo) and a respiratory effort transducer (BIOPAC), respectively. The pulse oximeter was placed on the subject’s left index finger, and the respiratory effort belt was placed around the subject’s abdomen. Physiological data were sampled at 40 samples per second using a multi-channel data acquisition board (National Instruments).

**Data analysis**

**Anatomical definition of noise ROI**

Anatomical data were segmented into gray matter, white matter, and CSF partial volume maps using the FAST algorithm available in the FSL software package (Smith et al., 2004). Tissue partial volume maps were linearly interpolated to the resolution of the functional data series using AFNI (Cox, 1996). In order to form white matter ROIs, the white matter partial volume maps were thresholded at a partial volume fraction of 0.99 and then eroded by two voxels in each direction to further minimize partial voluming with gray matter. CSF voxels were determined by first thresholding the CSF partial volume maps at 0.99 and then applying a three-dimensional nearest neighbor criteria to minimize multiple tissue partial voluming. Since CSF regions are typically small compared to white matter regions mask, erosion was not applied.

CSF and white matter ROIs were combined to form the anatomical noise ROI. Fig. 2 displays white matter and CSF ROIs for Subject 1, as denoted by the magenta voxels, overlaid on their respective partial volume maps. We refer to the application of CompCor with the anatomical noise ROI as aCompCor.

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**Fig. 2. Areas with a high fraction of white matter and cerebrospinal fluid (CSF), as denoted by the magenta voxels, overlaid on their respective partial volume maps from a representative slice from Subject 1. White-matter-only areas (panel a) were determined by first thresholding the white matter partial volume fraction map at 0.99 and then performing a map erosion by two pixels to minimize the effect of partial voluming with other tissue types. Panel b displays CSF-only areas with a partial volume fraction greater than 0.99 with application of a nearest neighbor clustering criteria.**
**tSTD-based determination of noise ROI**

In a preliminary abstract, Lund and Hanson (2001) showed that voxel time courses with a relatively high temporal standard deviation were dominated by physiological noise. They observed that these voxels occurred in edge regions, ventricles, and in areas close to large vessels. In their approach, they manually selected five pixels with high temporal standard deviation (tSTD) that appeared to represent physiological fluctuation. The time series from these voxels were then included as nuisance covariates in a GLM, resulting in a marked improvement in detection power (Lund and Hanson, 2001). Here we extend the prior work by first using the temporal standard deviation to select voxels in an unsupervised fashion and then using principal component analysis to reduce the dimensionality of the data. For each voxel time series, the temporal standard deviation is defined as the standard deviation of the time series after the removal of low-frequency nuisance terms (e.g., linear and quadratic drift). We denote the noise ROI determined in this fashion as the **tSTD noise ROI** and refer to the application of CompCor with this ROI as **tCompCor**.

To confirm that the tSTD metric identifies voxels with high levels of physiological noise, we first examined the relation between measures of physiological noise and tSTD. For each voxel, we defined the fractional variance of physiological noise as the ratio of the variance of the voxel time series accounted for by physiological noise regressors as determined with RETROICOR (see section on GLM analysis below) to the variance of the original time series after removal of constant and linear trends (e.g., the square of tSTD). The fractional variance of physiological noise was then compared to the temporal standard deviation on a per-voxel basis. Fig. 3 shows spatial maps of the fractional variance and tSTD (panels a and b respectively) as well as a plot of tSTD versus fractional variance for a representative slice from Subject 1. As demonstrated by the plot in panel c and the similarity of the spatial maps, the voxels with the highest tSTD also tend to have the highest fractional variance of physiological noise, confirming the observations of Lund and Hanson (2001).

To construct the tSTD noise ROI, we sorted the voxels by their temporal standard deviation and retained a pre-specified upper fraction of the sorted voxels within each slice. For example, specification of an upper fraction of 1% retains the voxels with the top 1% of temporal standard deviation values. Specification of the fraction involves a trade-off between including too few voxels to accurately represent the physiological noise space versus including too many voxels, which would tend to include voxels whose temporal standard deviation is not dominated by physiological noise. To empirically determine a reasonable value to use for the upper fraction, we computed the mean fractional variance of physiological noise across voxels within the tSTD ROI as a function of the upper fraction. This analysis was performed for each subject for both resting ASL and BOLD runs. Fig. 4 presents the mean across subjects of the fractional variance of physiological noise versus the fraction of included voxels. As a greater number

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**Fig. 3.** Panel a shows a spatial map of the fractional variance of physiological noise for the resting BOLD scan from a representative slice in Subject 1. Panel b shows a spatial map of the temporal standard deviation (tSTD). Areas of high fractional variance of physiological noise correspond to areas of high tSTD. Panel c compares the tSTD to the fractional variance of physiological noise on per-voxel basis. Data points in red represent the 2% of voxels in the slice with the highest tSTD.
of voxels are included in the analysis, the average fractional variance of physiological noise decreases for both ASL and BOLD resting runs. Both the ASL and BOLD curves show a steady decline in the fractional variance above a threshold of approximately 2%. Based on these results, we chose a 2% threshold (~20–30 voxels per slice) as a reasonable empirical threshold that effectively identified voxels with the highest fractional variance of physiological noise.

**Exclusion of stimulus-related components**

Although the construction of the noise ROIs is designed to include voxels that are unlikely to include stimulus-correlated activity, there is always a finite probability that some voxels may contain stimulus-related components. Inclusion of these voxels in the noise ROI will tend to reduce the statistical performance of the CompCor algorithm because stimulus-related components will be treated as physiological noise components. To minimize the probability of including voxels with stimulus-related components, we correlated the time course of each voxel within the noise ROI with the stimulus-related reference function and excluded any voxels with a p-value less than 0.2. To assess the effect of this threshold on performance, we performed Monte Carlo simulations to generate receiver operating characteristic (ROC) curves at various threshold levels and used the area under the ROC curve to quantify performance. An area of 1 represents ideal performance.

Simulated voxel responses (N=5000) were generated using the BOLD GLM presented in Eq. (1). Physiological regressors, P, were generated at frequencies consistent with cardiac (0.9 Hz) and respiration (0.3 Hz) with uniformly distributed phases to represent phase lags between voxels. Physiological noise weights, c, were chosen from a normal distribution N(0, 0.3). A constant term was included as a nuisance term with the regressor weight d chosen from a uniform distribution U(0, 1), and the additive white noise term, n, was generated from a normal distribution N(0, 1). The block stimulus paradigm was used to construct the stimulus design matrix X, and the stimulus weight h was set to a value of either 0 or 0.3 for the null and alternative hypotheses, respectively. Correlation of the simulated voxel responses with the block stimulus response was used to calculate p-values and z-scores for each condition. In the null hypothesis condition, the distribution of z-scores had a mean and standard deviation of ~0.31 and 0.89, respectively, whereas in the alternative hypothesis condition the mean and standard deviation were 3.18 and 1.27, respectively.

To construct the ROC curve, we varied the threshold on p-values from 0.01 to 1.0. For each threshold value, voxel time series with a p-value above the threshold were placed column-wise into a matrix M. A principal component analysis of the matrix M (see details in following section) was then used to form an estimate of the physiological noise matrix Phat. A GLM analysis of the simulated voxel time series was performed using the idealized stimulus response X and the computed Phat. The calculated p-values obtained under the null and alternative hypothesis conditions were then used to generate a ROC curve for each threshold value.

As the exclusion threshold was reduced from p=1.0 down to p=0.1, there was little degradation in detector performance (area under the ROC curve >0.99), since voxels with any hint of activation were effectively excluded. As the threshold was further reduced from 0.1 to 0.05, the ROC area decreased from 0.99 down to a value of 0.96, which is less than the area (0.98) obtained in the absence of CompCor (e.g., Phat not included in the GLM). The degradation in performance with lower p-values reflects the inclusion of weak stimulus-correlated components. Based on these findings, we chose a conservative threshold of p=0.2 to exclude voxels with stimulus-correlated fluctuations.

**Determination of principal components**

Voxel time series from the noise ROI (either anatomical or tSTD) were placed in a matrix M of size N×m, with time along the row dimension and voxels along the column dimension. The constant and linear trends of the columns in the matrix M were removed prior to column-wise variance normalization. The covariance matrix C=MM′ was constructed and decomposed into its principal components using a singular value decomposition.

The number of significant principal components to retain was determined using a modified version of the “broken stick" method described in Jackson (1993). This method identifies meaningful principal components (e.g., components unlikely to be due to random noise) by comparing their associated principal values to principal values derived from normally distributed data of equal rank. Ordered principal values calculated from normally distributed data tend to show a sharp initial decrease followed by a more gradual decrease, thus resembling a “broken-stick". In this method, a Monte Carlo simulation (N=1000) was first used to generate a statistical representation of expected principal values derived from normally distributed data of rank equal to the matrix M. This statistical distribution was then compared to the computed principal values from the data. Principal components that were significantly larger than the generated distribution, as assessed using a two-tailed t-test (p<0.05), were retained. Based on this method, we found an average of 6.3±0.52 and 4.5±0.38 significant principal components for BOLD and ASL runs, respectively, when using the anatomical noise ROI. For the tSTD noise ROI there were an average of 5.9±0.74 and 4.2±0.59 principal components for the BOLD and ASL runs, respectively.

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![Fractional Variance of Physiological Noise vs. % of Voxel (Sorted by tSTD) (N=10)](image-url)

Fig. 4. Mean fractional variance of physiological noise across subjects as a function of the fraction of voxels (sorted by tSTD) that is included in the noise ROI for BOLD (red) and ASL (blue) resting-state data. The black dotted line denotes the 2% threshold that is used in the present study.
**General linear model analysis**

All images were coregistered using AFNI software (Cox, 1996). Statistical inference was performed using a general linear model (GLM) analysis with an AR(1) model for the additive noise component (Broeck and Dale, 2000; Woolrich et al., 2001). The analysis was performed using the appropriate GLM for the BOLD and ASL time series under the following conditions: (1) no inclusion of physiological noise regressors (e.g., no correction), (2) inclusion of RETROICOR regressors, (3) inclusion of CompCor regressors derived from the anatomical noise ROI (aCompCor), and (4) inclusion of CompCor regressors derived from the TSTD noise ROI (tCompCor). The stimulus-related component $X_h$ was formed by convolving the appropriate stimulus pattern with a gamma density function of the form $h(t)=(πτ)^{-1/2}[(t−Δt)/τ]^{−(t−Δt)/τ}$ for $t≥Δt$ and 0 otherwise, with $τ=1.2$, $n=3$ and $Δt=1$ (Boynton et al., 1996). As nuisance regressors, we used a constant term, a linear term, and a discrete cosine set implemented in SPM2 with a minimum period of 120 s (Worsley and Friston, 1995; Lund et al., 2006). For statistical inference with RETROICOR, physiological noise regressors obtained from the cardiac and respiratory measurements were used to form the physiological noise matrix $P$ (Glover et al., 2000b; Restom et al., 2006). In addition, estimates of the cardiac and respiratory components were formed from partitioning the estimate of $Pc$ (i.e., $P_c C_c$ and $P_c R_c$ where the $C$ and $R$ subscripts denote cardiac and respiratory, respectively). For the application of aCompCor and tCompCor, GLM analysis was performed using noise matrix $P_{an}$, constructed from the principal component analysis of voxel time series from the anatomical noise ROI and the TSTD noise ROI, respectively. The estimate of the term $P_{an}$ was used as the CompCor estimate of the physiological noise component.

For each method, we formed a “corrected time series” by subtracting the estimates of the physiological noise components and the nuisance parameters from the measured time series. We then used these corrected time series to compute, on a per-subject basis, the mean temporal standard deviation of the resting-state data across all voxels within gray matter (partial volume $>0.9$). Paired $t$-tests (two-tailed) were used to assess differences between methods across the sample of subjects.

The number of activated voxels detected with each method was computed for each subject by thresholding the $F$-statistics at 5 and 30 for the ASL and BOLD functional runs, respectively. These values were chosen to yield approximately the same number of activated voxels for the ASL and BOLD functional runs and are consistent with thresholds previously used to investigate physiological noise reduction for ASL (Restom et al., 2006). Paired $t$-tests (two-tailed) were used to assess differences in the number of activated voxels.

**Spectral analysis**

We used spectral analysis to compare the physiological components estimated by RETROICOR with those estimated by CompCor. For each subject, we computed the power spectra of the physiological noise components estimated with each method on a per-voxel basis, normalized each power spectrum by its peak value, and then averaged the normalized spectra across all voxels in gray matter (partial volume $>0.9$). The RETROICOR power spectra were used to identify the peak cardiac and respiratory frequencies. We defined cardiac and respiratory frequency bands as the 0.1 Hz wide band of frequencies centered around the respective peak frequency. To quantify the similarity between methods of the spectra in these bands, we computed the band-averaged coherence $\text{Coh}_{xy}(f_{\text{band}})$ defined as

$$\text{Coh}_{xy}(f_{\text{band}}) = \frac{\sum_{f_{\text{band}}} S_{xx}(f) \sum_{f_{\text{band}}} S_{yy}(f)}{\sum_{f_{\text{band}}} S_{xx}(f) \sum_{f_{\text{band}}} S_{yy}(f)}$$

where $f_{\text{band}}$ denotes the frequency band, $x$ and $y$ are the two time series of interest, $S_{xx}(f)$ is the cross-spectrum of $x$ and $y$, and $S_{xx}(f)$ and $S_{yy}(f)$ are the power spectra of $x$ and $y$, respectively (Sun et al., 2004). The cross-spectral and power-spectral densities are estimated using Welch’s modified periodogram averaging method as previously outlined by Sun et al. (2004). Coherence is bounded by 0 and 1, with 1 representing perfect coherence, and is analogous to correlation analysis of time series. The spectral coherence between physiological noise elements was computed on a per-voxel basis and then averaged across gray matter voxels (partial volume $>0.9$).

**Additional analysis of BOLD data with TR of 2 s**

Although the physiological noise in the BOLD time series is critically sampled given the short TRs of 0.25 and 0.5 s for resting-state and functional runs, respectively, the cardiac and respiratory noise fluctuations in the ASL perfusion time series will typically be aliased due to the lower sampling rate (TR=2 s). In the results section we show that both aCompCor and tCompCor are capable of identifying these aliased components. To further demonstrate the performance of aCompCor and tCompCor for undersampled data, we downsampled the data by factors of 4 and 8 for the functional and resting-state runs, respectively, to generate BOLD time series with a TR of 2 s and analyzed the performance of the CompCor methods using the GLM analysis approach described above. We also applied CompCor to the BOLD-weighted second echo data from the ASL time series (TR of 2 s), using the GLM in Eq. (2) with $b_{\text{BOLD}}$ as the parameter of interest.

**Receiver operating characteristic curve**

To gain additional insight into the relative performance of the CompCor methods, we used simulations to construct receiver operating characteristic (ROC) curves. For these simulations, we first defined a region of interest (ROI) in the visual cortex based on GLM analysis (with tCompCor regressors) of the 2nd echo BOLD data from the block design functional runs. For each subject, a liberal threshold ($r>0.2$) was used to delimit an ROI with approximately 400 to 500 voxels. These voxels were then used for the subsequent simulations, which made use of the BOLD resting-state data. For each method, the false positive rates at varying thresholds were calculated by applying the GLM analysis to the resting-state data and computing the fraction of false positives within the ROI. To determine the true positive rates, we added simulated activations (block design: 20 s on, 40 s off; 1% amplitude) to the time course of each voxel within the ROI. At each threshold level, we then computed the fraction of true positives within the ROI.

**Performance of tCompCor in the presence of motion**

As the tCompCor approach is based on the identification of voxel time series with high temporal standard deviations, it will also identify voxels with large signal components due to subject motion. Motion-related signal changes can reflect both simple linear effects (e.g., translation and rotation of brain regions) and
more complex nonlinear effects, such as changes in the distortion and blurring of the image due to magnetic field inhomogeneities. To the extent that motion-related signal changes increase the temporal standard deviation of the time series, these changes can be reflected in the principal components identified by tCompCor. In the presence of stimulus-correlated motion, the exclusion process described previously will bias against the inclusion of time series with stimulus-correlated changes. As a demonstration of the application of tCompCor in the presence of subject motion, we analyzed a BOLD (TR = 0.5 s) time series in which there was significant subject motion. The data were acquired during a periodic single trial run with the protocol and imaging parameters described above. To emphasize the effect of motion, we applied tCompCor to data that were not motion corrected. Estimates of rotation and displacement during the experiment were obtained with the 3dvolreg program in AFNI.

Results

Fig. 5 shows normalized power spectra of physiological components estimated by RETROICOR, aCompCor, and tCompCor for the resting-state BOLD run of Subject 1. The top row (panel a) depicts the respiratory and cardiac components identified with the use of RETROICOR. Cardiac and respiratory peaks are located prominently at ~1.2 Hz and ~0.2 Hz, respectively. Panels b and c show the average spectra of elements estimated by aCompCor and tCompCor, respectively. Both variants of CompCor estimate cardiac and respiratory elements that are similar to those removed by RETROICOR. In addition, very low frequency 1/f components are visible in both the aCompCor and tCompCor spectra. These low-frequency components can appear in the CompCor spectra because we remove only constant and linear trend terms prior to the principal component analysis. Note that, as stated in the Methods section, the use of the discrete cosine transform (DCT) low-frequency nuisance terms is reserved for the statistical assessments performed with the GLM. As a result, the space spanned by the principal components may partially overlap with the space spanned by the discrete cosine transform nuisance terms. Potential issues with this overlap are addressed in the Discussion section.

Fig. 6 shows the average spectra from Subject 1 of the noise elements estimated from the resting-state ASL data. In the top row, the RETROICOR estimated cardiac (red line) and respiratory (green line) elements are aliased due to the long TR. The spectrum of elements estimated by either aCompCor (panel b) and tCompCor (panel c) shows components consistent with the cardiac and respiratory elements identified by RETROICOR.

![Fig. 5. Average normalized power spectra of components estimated with the application of various correction schemes to the resting BOLD run from Subject 1. As shown in panel a, cardiac and respiratory elements estimated by RETROICOR are located at 1.2 and 0.2 Hz, respectively. Application of aCompCor (panel b) or tCompCor (panel c) estimates components similar to the cardiac and respiratory elements identified by RETROICOR.](image-url)
To quantify the similarity between the spectra, we used the spectral coherence analysis described above in Methods. For aCompCor applied to the resting BOLD runs, the average spectral coherence and standard error values across subjects ($N=10$) were $0.67 \pm 0.08$ and $0.80 \pm 0.05$ for respiratory and cardiac elements, respectively. Corresponding values for tCompCor were $0.62 \pm 0.10$ and $0.86 \pm 0.07$. For resting ASL runs the mean spectral coherences when using aCompCor were $0.79 \pm 0.03$ and $0.65 \pm 0.06$ for respiratory and cardiac elements, respectively, with corresponding values of $0.82 \pm 0.03$ and $0.69 \pm 0.06$ for tCompCor.

The effects of CompCor and RETROICOR on the average temporal standard deviation (tSTD) of the resting BOLD and ASL data are shown in Fig. 7, with associated standard error bars. The panels show the normalized mean temporal standard deviation (tSTD) in gray matter (partial voluming $>0.9$) for (a) resting TR = 0.25 s BOLD data, (b) downsampled (TR = 2 s) resting BOLD data, (c) resting 1st echo ASL (perfusion) data, and (d) resting 2nd echo BOLD data, with the application of RETROICOR and the two variants of CompCor. For each subject, the tSTD values obtained with physiological noise reduction methods are normalized by the values obtained for the uncorrected time series. The standard error bars are provided to give a sense of the inter-subject variability, but should not be used to interpret statistical significance, since paired t-tests are used to compare the normalized tSTD values between methods.

As compared to no correction, RETROICOR significantly ($p<0.001$) reduced the normalized tSTD in the resting (TR = 0.25 s) BOLD data by 8% whereas application of aCompCor and tCompCor resulted in even greater reductions of 20% ($p<0.001$) and 29% ($p<0.001$), respectively. Both variants of CompCor significantly ($p<0.02$) reduced the tSTD as compared to RETROICOR, and tCompCor significantly ($p<0.001$) reduced the tSTD compared to aCompCor. For the downsampled (TR = 2 s) BOLD data, all three methods significantly ($p<0.001$) reduced the normalized tSTD with percent decreases of 12%, 17% and 22% for RETROICOR, aCompCor, and tCompCor, respectively. In addition, the normalized tSTD values achieved with tCompCor were significantly ($p<0.03$) lower than the values obtained with either RETROICOR or aCompCor.

For the resting 1st echo ASL data, all three methods significantly ($p<0.001$) reduced the normalized tSTD with percent decreases of 13%, 18%, and 23%. The normalized tSTD values obtained with aCompCor and tCompCor were significantly ($p<0.04$) lower than the values obtained with RETROICOR. In addition, the tSTD obtained with tCompCor were significantly ($p<0.03$) lower than the
values obtained with aCompCor. Similarly, for the resting 2nd echo BOLD data, the three methods led to significant ($p < 0.001$) reductions in tSTD with percent decreases of 13%, 19%, and 21%. Both aCompCor and tCompCor lead to significantly greater reductions ($p < 0.01$) than RETROICOR.

Bar graphs comparing the effect of the various correction schemes on the normalized number of activated voxels for the BOLD periodic and functional ASL block runs are shown in Fig. 8. For each method, the number of activated voxels is normalized on a per-subject basis by the number of voxels detected for the data prior to the application of noise reduction. As with the plots in Fig. 7, since statistical significance is assessed with paired tests, the standard errors bars are provided only to give a sense of inter-subject variability. As compared to no correction, there were significant ($p < 0.02$) increases of 10%, 76% and 82% in the normalized number of activated voxels for the periodic (TR=0.5 s) BOLD runs (panel a) with the application of RETROICOR, aCompCor, and tCompCor, respectively. Application of either aCompCor or tCompCor increased the number of voxels significantly ($p < 0.04$) as compared to RETROICOR. For the downsampled (TR=2 s) BOLD data, both aCompCor and tCompCor significantly increased the normalized number of activated voxels with respect to both the uncorrected data ($p < 0.005$) and RETROICOR ($p < 0.005$).

Fig. 9 shows a representative ROC curve comparing the relative performances achieved without correction (blue) and the application of RETROICOR (green), aCompCor (red), and tCompCor (cyan). Consistent with the results shown in Fig. 8, both aCompCor and tCompCor yield better detection performance than RETROICOR, and the performance of tCompCor is better than that of aCompCor.

Fig. 10 shows an example of the performance of tCompCor in the presence of signal changes due to subject motion. The top row shows the uncorrected BOLD time series (red), the time series after application of tCompCor (blue), and the periodic single trial reference function (black dash line). For this run, the most significant motion components were found to be left–right roll and displacement. Estimates of roll in units of degrees (blue) and displacement in units of millimeters (green) are shown in the middle row. Note that the large motion peaking at 79 s gives rise to a large signal change in the uncorrected time series. The bottom row shows the top three principal components as estimated by tCompCor. These components reflect the motion at 79 s as well as smaller movements in other portions of the experimental run.
Projecting these components out of the uncorrected time series leads to the corrected time series, with a noticeable reduction in the motion-related signal changes, especially at the 79-s timepoint.

Discussion

In this paper, we have examined whether signal components derived from regions of interest that are unlikely to be modulated by neural activity can be used to estimate noise components (due to physiological fluctuations, subject motion, etc.) within activated regions. We considered two methods for the determination of the noise ROIs: (1) anatomical identification of significant areas of CSF and white matter and (2) definition of noise regions based upon their temporal standard deviation. We demonstrated that the application of CompCor using either ROI significantly reduces the temporal standard deviation of both resting-state BOLD and ASL data. Additionally, we have shown that CompCor using either ROI leads to a marked improvement in sensitivity to detect the response to a visual stimulus, as quantified by the number of significantly activated voxels for both BOLD and ASL experiments.

For the resting-state data, we found a significantly greater reduction of the normalized temporal standard deviation with the application of CompCor as compared to RETROICOR (with the exception of aCompCor for the downsampled BOLD data). This is most likely due to the removal of noise terms that are identified by the principal component analysis used in CompCor but not modeled by the RETROICOR cardiac and respiratory regressors.

For the functional BOLD runs, we found that the application of either aCompCor or tCompCor resulted in significantly more activated voxels as compared to RETROICOR. In contrast, for the ASL data, there were not significant differences between the percent...
of activated voxels detected by either form of CompCor as compared to RETROICOR. Due to the tag and control modulation used in the ASL acquisition process, low-frequency noise components are effectively attenuated in the ASL analysis process (Liu and Wong, 2005). The fact that the improved detection performance of the CompCor methods was limited to the BOLD data suggests that the gain reflects a reduction in low-frequency noise components that are identified by CompCor but not by RETROICOR. As noted in the Results section, the presence of these low-frequency components may cause the space spanned by the principal components to overlap with the signal space spanned by the nuisance regressors used in the general linear model. In the unlikely case that the overlap causes the model to be ill-posed, it may be necessary to orthogonalize the principal components with respect to the nuisance regressors. However, we have not found this to be necessary in practice.

The performance gains achieved with both RETROICOR and CompCor (as compared to the uncorrected data) were observed both for the critically sampled (TR = 0.25 s and 0.5 s) BOLD data and for the undersampled or downsampled (TR = 2 s) ASL and BOLD data. In the undersampled data, both respiratory and cardiac fluctuations are typically aliased. With RETROICOR, these aliased components can be identified from the external measures of cardiac and respiratory activity, as has been previously discussed (Glover et al., 2000b; Restom et al., 2006). In CompCor, the principal component analysis takes advantage of the spatial coherence of the aliased components to identify the most significant aliased components. Because this identification procedure does not depend on the frequencies of the physiological components, it works well even with undersampled data. As shown by Fig. 6 and the spatial coherence measures reported in the Results section, both RETROICOR and CompCor identify similar spectral components in both the critically sampled and undersampled data.

The ability of CompCor to identify spatially coherent noise components that are unlikely to be of neural origin also plays a role in its capacity to improve performance in the presence of motion-related signal changes. Since these effects are primarily due to bulk motion, they will tend to give rise to spatially coherent signal changes. Although the exact signal change in any given voxel will depend on a variety of factors, such as the local anatomy and magnetic field distributions, CompCor will identify those components that are common across voxels. The performance of CompCor in any given voxel will depend on the extent to which these components can represent the signal changes in that voxel. An example of the efficacy of tCompCor in removing a motion-related signal component is shown in Fig. 10. In cases with especially severe motion artifacts, the principal components identified by CompCor may primarily describe the effects of motion, thus possibly decreasing the ability of CompCor to reduce the effect of cardiac and respiratory fluctuations. Further work to better elucidate the limitations of CompCor in the presence of motion would be useful.

The accurate specification of the noise ROI is key to both aCompCor and tCompCor. As discussed in the Methods section, inclusion of voxels with stimulus-correlated activity can reduce the performance of the methods. For aCompCor this may occur due to factors such as inaccuracies in tissue segmentation or misalignment of the anatomical and functional data (e.g., due to subject movement between the scans). For tCompCor this performance reduction can occur when voxels with high tSTD also have significant stimulus-correlated components (e.g., due to stimulus-correlated motion). In the present study, we used a liberal threshold ($p < 0.2$) to exclude voxels with possible stimulus-correlated components. Although our experimental data support the efficacy of this approach for periodic and block designs, the performance of
this approach may be reduced for complex event-related fMRI experiments in which the expected stimulus-related response may not be well defined. In addition, in the rare cases where the cardiac noise is aliased to the stimulus frequency (Lund and Hanson, 2001), the exclusion criteria will reduce the ability of CompCor to identify these noise sources. Finally, this exclusion approach is not easily extended to resting-state experiments aimed at studying functional connectivity. Future work addressing the applicability of CompCor to these types of studies would be useful.

In this work we used an empirical threshold to determine the fraction of voxels to retain in the TSTD noise ROI. While this threshold provided better performance for the datasets analyzed in this study, it is possible that this threshold may not be optimum for other datasets. An examination of additional datasets would be helpful for better characterizing the efficacy of tCompCor. In addition, an investigation into other approaches for determining the threshold may provide gains in performance.

Conclusion

We have shown that application of CompCor to ASL and BOLD fMRI time series can significantly reduce noise due to physiological fluctuations and other sources, such as subject motion. CompCor does not require external monitoring and can be applied in an automated fashion to reduce the confounding effect of physiological fluctuations on fMRI time series.

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References


