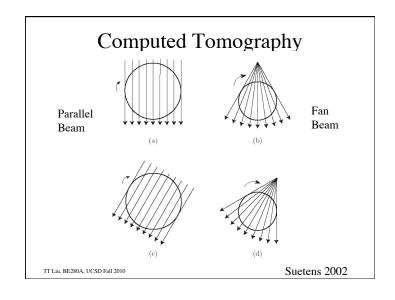
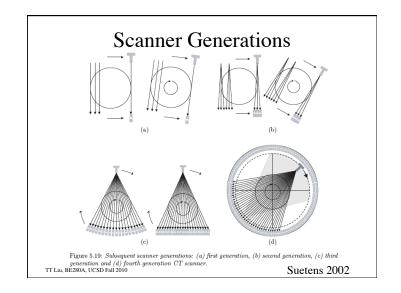
### Bioengineering 280A Principles of Biomedical Imaging

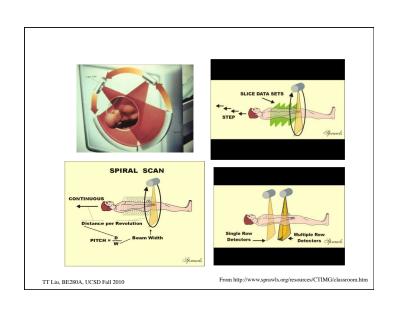
Fall Quarter 2010 CT Lecture 1

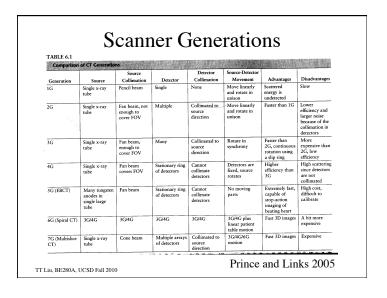
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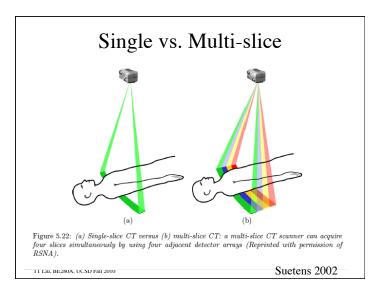
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### 1G vs. 2G scanner

Example 6.1 from Prince and Links.

 $Compare\ 1G\ \ vs.\ 2G\ scanner\ whose\ source-\ detector\ apparatus\ can\ move\ linearly$ 

at speed of 1 m/sec; FOV 0.5m; 360 projections over 180 degrees; 0.5 s for apparatus

to rotate one angular increment, regardless of angle.

 $Question: \ \, Scan \ time \ for \ 1\ G\ scanner?\ \, Scan \ time \ for \ 2G\ scanner \ with \ 9\ detectors\ space\ 0.5$ 

degrees apart?

Answer

1G scanner: 0.5m/(1m/s) = 0.5s per projection.

360\*0.5 = 180s scan time

360\*0.5 = 180s for rotation of apparatus.

Total time = 360 s or 6 minutes.

2G scanner: Required angular resolution is 180/360 = 0.5 degrees -- agrees with spacing.

360/9 = 40 rotations required. 40\*0.5 = 20s for scanning

40\*0.5 = 20s for scanning 40\*0.5 = 20s for rotations.

Total time = 40s.

## 3G, 6G, and 7G scanners

3G scanner: Typical scanner acquires 1000 projections with fanbeam angle of 30 to 60 degrees; 500 to 700 detectors; 1 to 20 seconds.

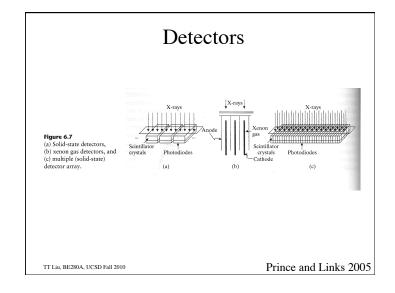
6G: Spiral/Helical CT

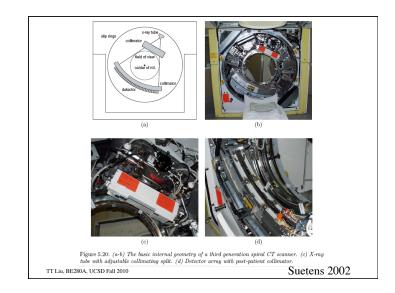
60 cm torso scan: 30s. 24 cm lung scan: 12s 15 cm angio: 30s

7G: Multislice CT

64 or more parallel 1D projections.

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# CT Line Integral

$$I_d = \int_0^{E_{\text{max}}} S_0(E) E \exp\left(-\int_0^d \mu(s; E') ds\right) dE$$

Monoenergetic Approximation

$$I_d = I_0 \exp\left(-\int_0^d \mu(s; \overline{E}) ds\right)$$

$$g_{d} = -\log\left(\frac{I_{d}}{I_{0}}\right)$$
$$= \int_{0}^{d} \mu(s, \overline{E}) ds$$

## CT Number

$$CT_number = \frac{\mu - \mu_{water}}{\mu_{water}} \times 1000$$

Measured in Hounsfield Units (HU)

Air: -1000 HU

Soft Tissue: -100 to 60 HU Cortical Bones: 250 to 1000 HU Metal and Contrast Agents: > 2000 HU

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# Direct Inverse Approach

$\mu_1$	$\mu_2$	$p_1$	$p_1 = \mu_1 + \mu_2$	$\begin{bmatrix} p_1 \\ p_2 \\ p_3 \\ p_4 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \end{bmatrix}$	1	0	$\begin{bmatrix} 0 \\ \mu_1 \end{bmatrix} \begin{bmatrix} \mu_1 \\ \mu_2 \end{bmatrix}$
$\mu_3$	$\mu_4$	$p_2$	$p_2 = \mu_3 + \mu_4$ $p_3 = \mu_1 + \mu_3$	$\begin{vmatrix} p_2 \\ p_3 \end{vmatrix} = \begin{vmatrix} 0 \\ 1 \end{vmatrix}$	0	1	$0 \begin{vmatrix} \mu_2 \\ \mu_3 \end{vmatrix}$
$p_3$	$p_4$	_	$p_4 = \mu_2 + \mu_4$	$\lfloor p_4 \rfloor \lfloor 0$	1	0	$1 \parallel \mu_4 \rfloor$

4 equations, 4 unknowns.

Are these the correct equations to use?

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### CT Display

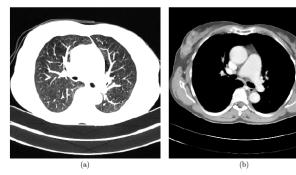


Figure 5.4: CT-image of the chest with different window/level settings:(a) for the lungs (window 1500 and level -500) and (b) for the soft tissues (window 350 and level 50).

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## Direct Inverse Approach

$\mu_1$ $\mu_3$	$\mu_2$ $\mu_4$	$p_1$ $p_2$	$p_{1} = \mu_{1} + \mu_{2}$ $p_{2} = \mu_{3} + \mu_{4}$ $p_{3} = \mu_{1} + \mu_{3}$ $p_{4} = \mu_{2} + \mu_{4}$	$\begin{bmatrix} p_1 \\ p_2 \\ p_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$	1 0 0	0 1 1	$ \begin{array}{c c} 0 & \mu_1 \\ 1 & \mu_2 \\ 0 & \mu_3 \end{array} $
p <sub>3</sub>	p <sub>4</sub>		$p_4 = \mu_2 + \mu_4$	$\lfloor p_4 \rfloor \ \lfloor 0$	1	0	$1 \  \mu_4 \ $

4 equations, 4 unknowns.

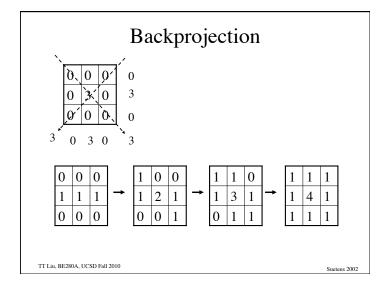
Are these the correct equations to use?

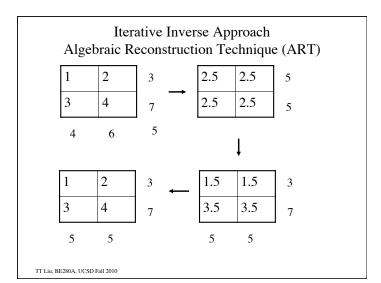
## Direct Inverse Approach

$\mu_1$	$\mu_2$	$p_1$	$p_1 = \mu_1 + \mu_2$	$ \begin{bmatrix} p_1 \\ p_2 \\ p_3 \\ p_5 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 1 \end{bmatrix} $	1	0	$\begin{bmatrix} 0 \\ \mu_1 \end{bmatrix} \begin{bmatrix} \mu_1 \\ \mu_2 \end{bmatrix}$
$\mu_3$	$\mu_4$	$p_2$	$p_2 = \mu_3 + \mu_4$ $p_3 = \mu_1 + \mu_3$	$\begin{vmatrix} p_2 \\ p_3 \end{vmatrix} = \begin{vmatrix} 0 \\ 1 \end{vmatrix}$	0	1	$0 \begin{vmatrix} \mu_2 \\ \mu_3 \end{vmatrix}$
p <sub>o</sub>	D,	<b>–</b> n.	$p_5 = \mu_1 + \mu_4$	$\lfloor p_5 \rfloor$ [1	0	0	$1 \  \mu_4 \ $

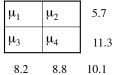
4 equations, 4 unknowns. These are linearly independent now. In general for a NxN image,  $N^2$  unknowns,  $N^2$  equations. This requires the inversion of a  $N^2xN^2$  matrix For a high-resolution 512x512 image,  $N^2$ =262144 equations. Requires inversion of a 262144x262144 matrix! Inversion process sensitive to measurement errors.

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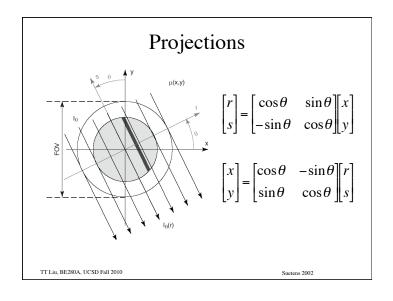


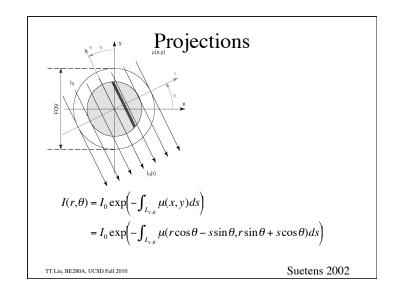


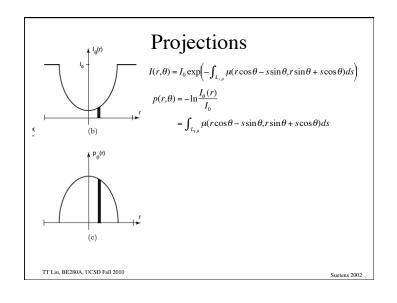


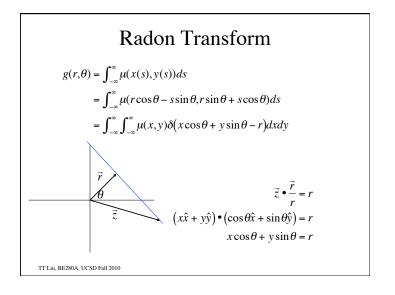
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# Example

$$f(x,y) = \begin{cases} 1 & x^2 + y^2 \le 1 \\ 0 & \text{otherwise} \end{cases}$$

$$g(l,\theta = 0) = \int_{-\infty}^{\infty} f(l,y) dy$$
$$= \int_{-\sqrt{l-l^2}}^{\sqrt{l-l^2}} dy$$
$$= \begin{cases} 2\sqrt{1-l^2} & |l| \le 1\\ 0 & \text{otherwise} \end{cases}$$

