

Bioengineering 280A
Principles of Biomedical Imaging

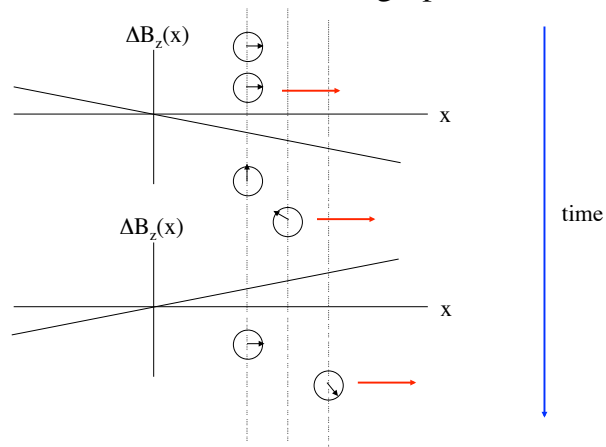
Fall Quarter 2010
MRI Lecture 6

Moving Spins

So far we have assumed that the spins are not moving (aside from thermal motion giving rise to relaxation), and contrast has been based upon T_1 , T_2 , and proton density. We were able to achieve different contrasts by adjusting the appropriate pulse sequence parameters.

Biological samples are filled with moving spins, and we can also use MRI to image the movement. Examples: blood flow, diffusion of water in the white matter tracts. In addition, we can also sometimes induce motion into the object to image its mechanical properties, e.g. imaging of stress and strain with MR elastography.

Phase of Moving Spin



Phase of a Moving Spin

$$\begin{aligned}
 \varphi(t) &= -\int_0^t \Delta\omega(\tau) d\tau \\
 &= -\int_0^t \gamma \Delta B(\tau) d\tau \\
 &= -\int_0^t \gamma \vec{G}(\tau) \cdot \vec{r}(\tau) d\tau \\
 &= -\gamma \int_0^t [G_x(\tau)x(\tau) + G_y(\tau)y(\tau) + G_z(\tau)z(\tau)] d\tau
 \end{aligned}$$

Phase of Moving Spin

Consider motion along the x-axis

$$x(t) = x_0 + vt + \frac{1}{2}at^2$$

$$\begin{aligned} \varphi(t) &= -\gamma \int_0^t G_x(\tau) x(\tau) d\tau \\ &= -\gamma \int_0^t G_x(\tau) \left[x_0 + v\tau + \frac{1}{2}a\tau^2 \right] d\tau \\ &= -\gamma \left[x_0 \int_0^t G_x(\tau) d\tau + v \int_0^t G_x(\tau) \tau d\tau + \frac{a}{2} \int_0^t G_x(\tau) \tau^2 d\tau \right] \\ &= -\gamma \left[x_0 M_0 + v M_1 + \frac{a}{2} M_2 \right] \end{aligned}$$

Phase of Moving Spin

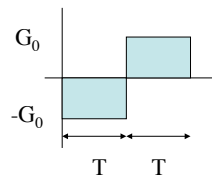
$$\varphi(t) = -\gamma \left[x_0 M_0 + v M_1 + \frac{a}{2} M_2 \right]$$

$$M_0 = \int_0^t G_x(\tau) d\tau \quad \text{Zeroth order moment}$$

$$M_1 = \int_0^t G_x(\tau) \tau d\tau \quad \text{First order moment}$$

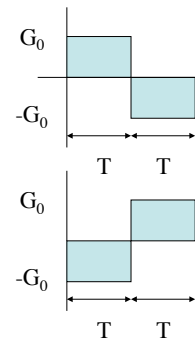
$$M_2 = \int_0^t G_x(\tau) \tau^2 d\tau \quad \text{Second order moment}$$

Flow Moment Example



$$\begin{aligned} M_0 &= \int_0^t G_x(\tau) d\tau = 0 \\ M_1 &= \int_0^t G_x(\tau) \tau d\tau \\ &= -\int_0^T G_0 \tau d\tau + \int_T^{2T} G_0 \tau d\tau \\ &= G_0 \left[-\frac{\tau^2}{2} \Big|_0^T + \frac{\tau^2}{2} \Big|_T^{2T} \right] \\ &= G_0 \left[-\frac{T^2}{2} + \frac{4T^2}{2} - \frac{T^2}{2} \right] = G_0 T^2 \end{aligned}$$

Phase Contrast Angiography (PCA)



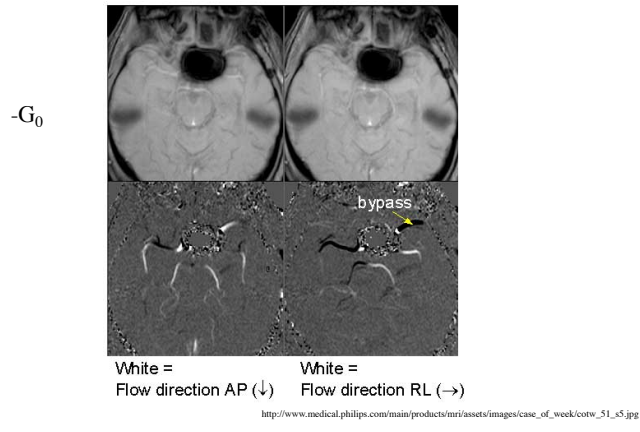
$$\varphi_1 = -\gamma v_x M_1 = \gamma v_x G_0 T^2$$

$$\varphi_2 = -\gamma v_x M_1 = -\gamma v_x G_0 T^2$$

$$\Delta\varphi = \varphi_1 - \varphi_2 = 2\gamma v_x G_0 T^2$$

$$v_x = \frac{\Delta\varphi}{2G_0 T^2}$$

PCA example

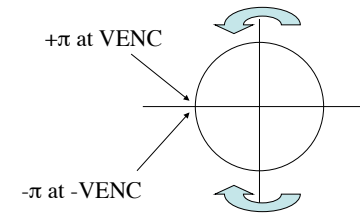


Aliasing in PCA

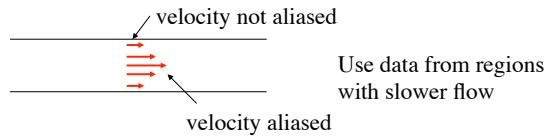
Define VENC as the velocity at which the phase is 180 degrees.

$$VENC \equiv \frac{\pi}{\gamma G_0 T^2}$$

Because of phase wrapping the velocity of spins flowing faster than VENC is ambiguous.



Aliasing Solutions



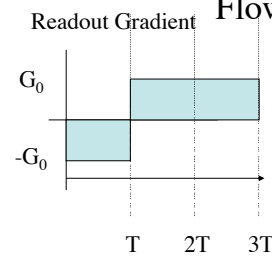
Use multiple VENC values so that the phase differences are smaller than π radians.

$$\varphi_1 = \pi \frac{v_x}{VENC_1}$$

$$\varphi_2 = \pi \frac{v_x}{VENC_2}$$

$$\varphi_1 - \varphi_2 = \pi v_x \left(\frac{1}{VENC_1} - \frac{1}{VENC_2} \right)$$

Flow Artifacts



During readout moving spins within the object will accumulate phase that is in addition to the phase used for imaging. This leads to

- 1) Net phase at echo time TE = 2T.
- 2) An apparent shift in position of the object.
- 3) Blurring of the object due to a quadratic phase term.

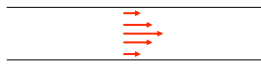
Flow Artifacts

Plug Flow



All moving spins in the voxel experience the same phase shift at echo time.

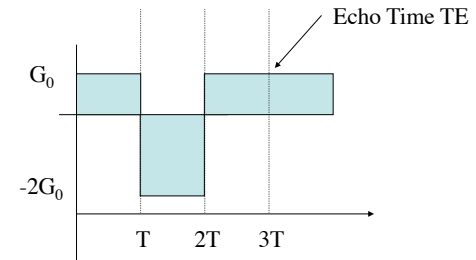
Laminar Flow



Spins have different phase shifts at echo time. The dephasing causes the cancellation and signal dropout.

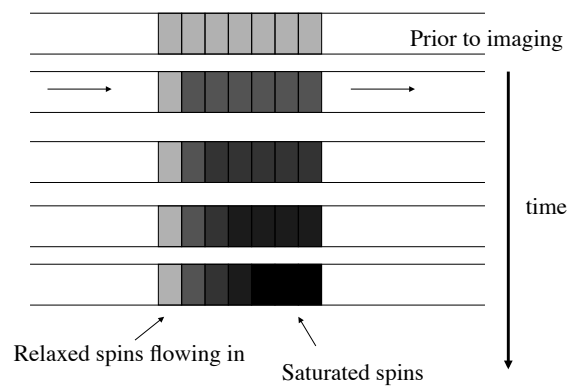
Flow Compensation

Readout Gradient

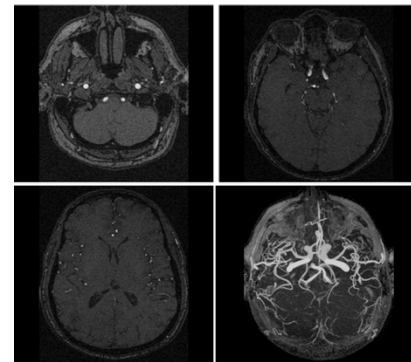


At TE both the first and second order moments are zero, so both stationary and moving spins have zero net phase.

Inflow Effect



Time of Flight Angiography

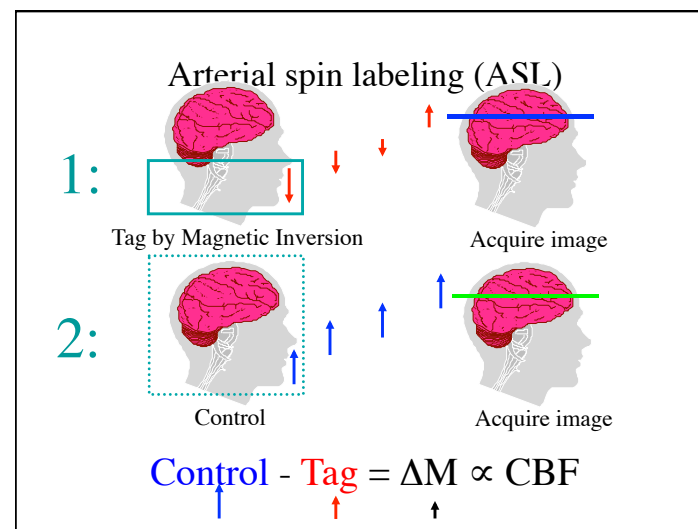
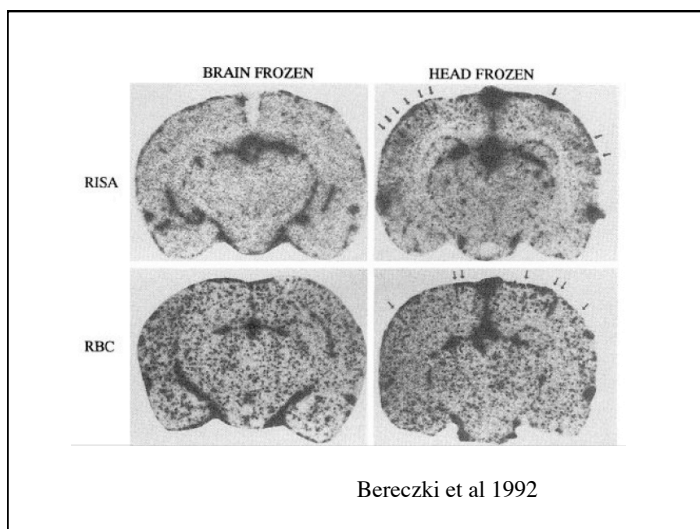
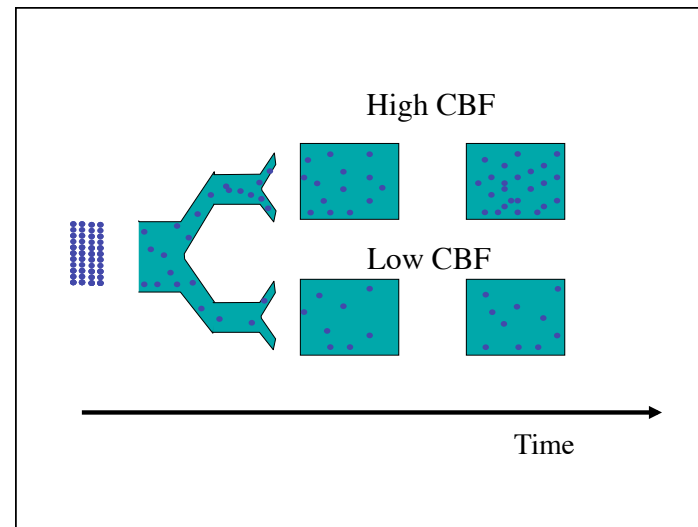


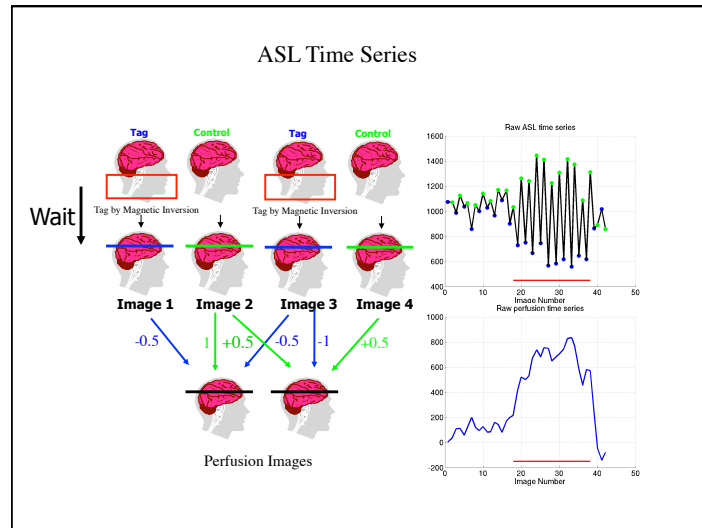
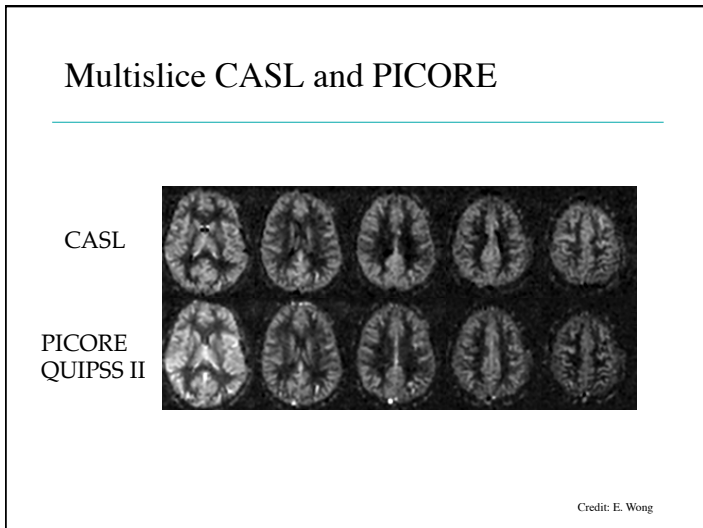
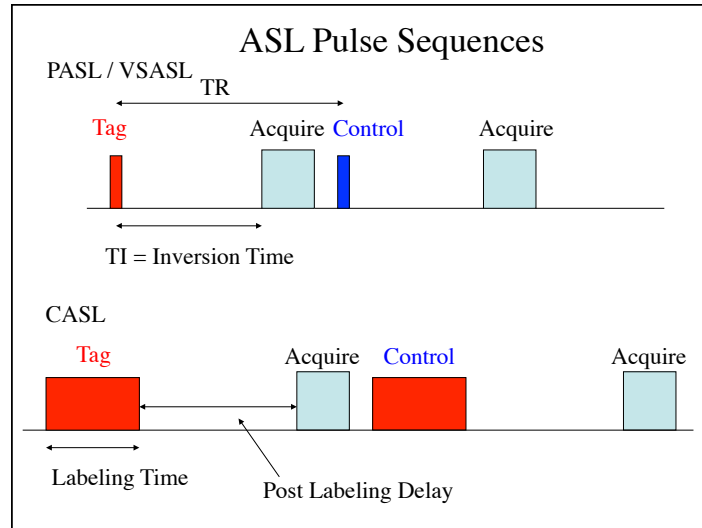
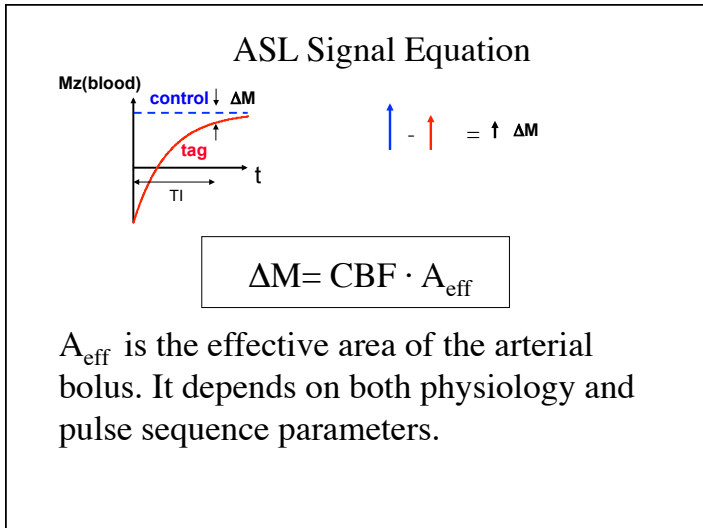
Cerebral Blood Flow (CBF)

CBF = Perfusion
 = Rate of delivery of arterial blood to a capillary bed in tissue.

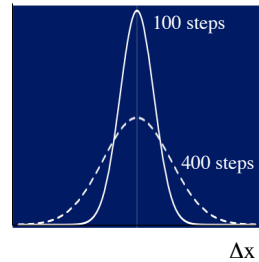
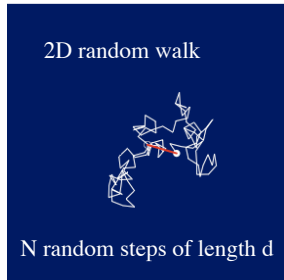
Units: $\frac{\text{ml of Blood}}{(100 \text{ grams of tissue})(\text{minute})}$

Typical value is 60 ml(100g-min) or
 60 ml(100 ml-min) = 0.01 s^{-1} , assuming
 average density of brain equals 1 gm/ml





Diffusion



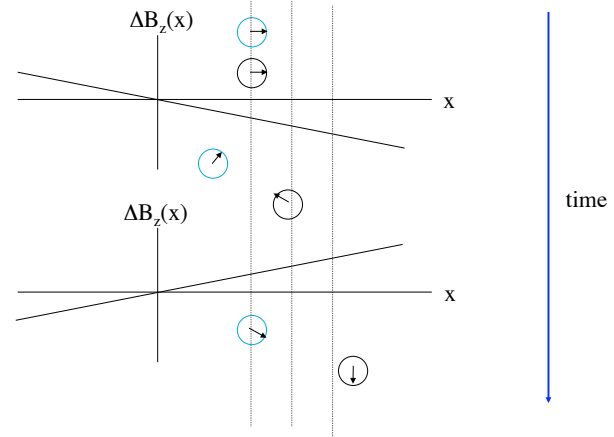
$$\langle \Delta x^2 \rangle = Nd^2 = 2DT$$

D = diffusivity

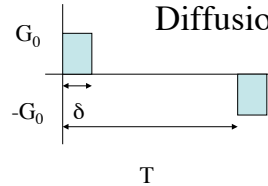
In brain:
 $D \approx 0.001 \text{ mm}^2/\text{s}$
 For $T=100 \text{ msec}$,
 $\Delta x \approx 15 \mu$

Credit: Larry Frank

Diffusing Spins



Diffusion Weighting



Signal

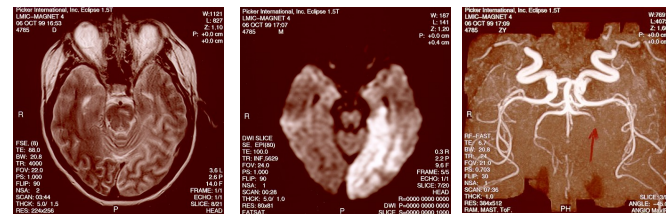
$$S \propto e^{-\gamma^2 G_0^2 \delta^2 DT} = e^{-bD}$$

where $b = \gamma^2 G_0^2 \delta^2 (T - \delta/3)$

Diffusivity

Diffusion Weighted Images

T2 weighted Diffusion Weighted Angiogram

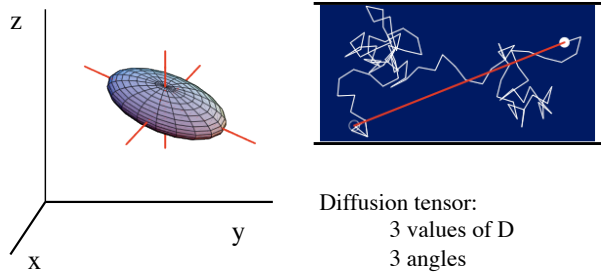


After a stroke, normal water movement is restricted in the region of damage. Diffusivity decreases, so the signal intensity increases.

<http://lehighmri.com/cases/dwi/patient-b.html>

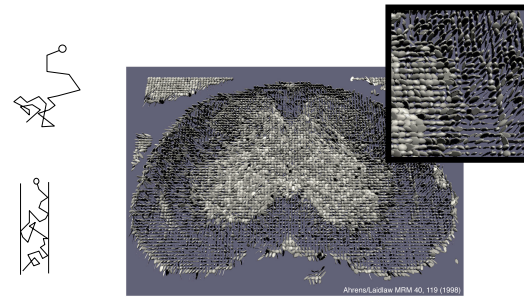
Restricted Diffusion

D depends on direction

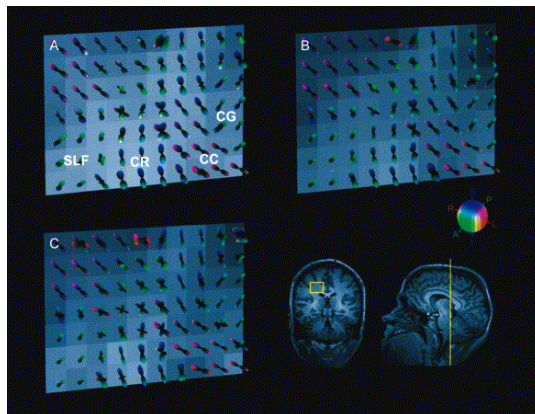


Credit: Larry Frank

Diffusion Imaging Example

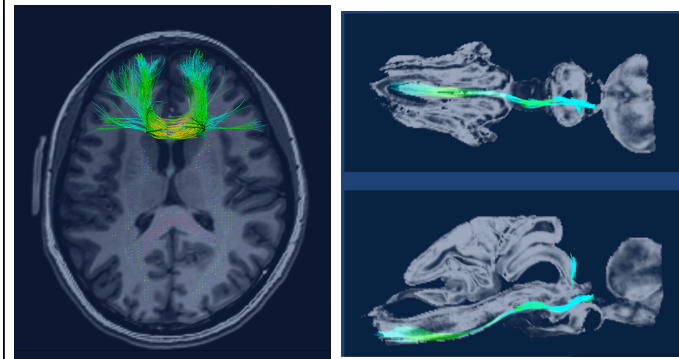


Q-ball imaging



Tuch et al, Neuron 2003

Fiber tract mapping of neural connectivity



Courtesy of L. Frank